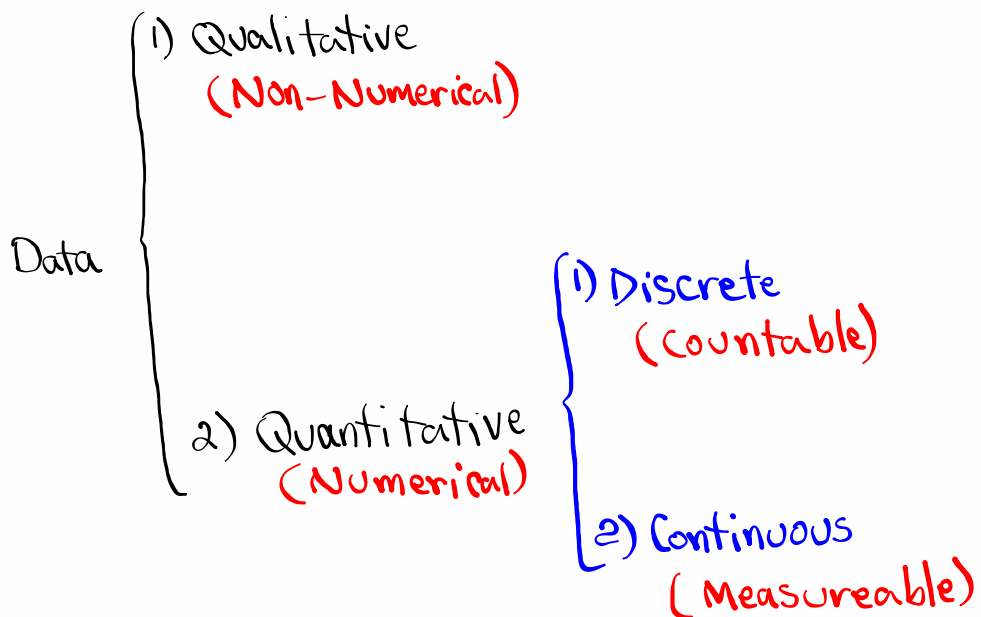


# Statistics

## Lecture 8



Feb 19-8:47 AM



Oct 17-6:52 PM

Let  $x$  be a discrete random variable with  
 Prob. dist. of  $P(x)$ :

what is Prob. dist.?

It is a way to give prob. of all  
 possible outcomes.

- 1) It could be in the form of a chart or table.
- 2) It could be in the form of a graph
- 3) It could be in using some formulas.
- 4) It could be computed using Traditional Prob.

Oct 17-6:54 PM

Consider  $x$  with Prob. dist.  $P(x)$

- 1)  $0 \leq P(x) \leq 1$
- 2)  $\sum P(x) = 1$
- 3)  $P(x) = 1 \iff$  Sure event
- 4)  $P(x) = 0 \iff$  Impossible event
- 5)  $0 < P(x) \leq .05 \iff$  Rare event

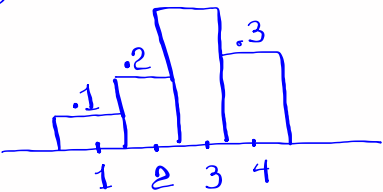
Oct 17-6:58 PM

Consider the chart below

$x$	$P(x)$
1	.1
2	.2
3	.4
4	.3

1) Verify  $\sum P(x) = 1$   
 $.1 + .2 + .4 + .3 = 1 \checkmark$

2) Draw Prob. dist. Histogram  
 $x \rightarrow$  Midpoint  
 $P(x) \rightarrow$  Rel. F. .4



clear all lists  
 Reset all lists  
 $x \rightarrow$  L1,  $P(x) \rightarrow$  L2  
 use 1-Var Stats with  
 L1 & L2, find  $\bar{x} = 2.9$   
 $S_x =$  blank  
 $n = 1 \leftarrow$  Total Prob. = 1

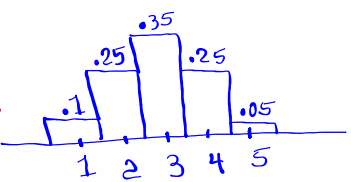
Oct 17-7:01 PM

use the chart below for discrete random variable  $x$  with prob. dist.  $P(x)$

$x$	$P(x)$
1	.1
2	.25
3	.35
4	.25
5	.05

1) Find  $P(x=5)$   
 $P(x=5) = 1 - [.1 + .25 + .35 + .25]$   
 $\uparrow$   
 Total Prob. =  $1 - .95 = .05$

2) Draw Prob. dist. histogram  
 $x \rightarrow$  Midpoint,  $P(x) \rightarrow$  Rel. F.



clear all lists  
 $x \rightarrow$  L1,  $P(x) \rightarrow$  L2  
 use 1-Var Stats with  
 L1 & L2, find  $\bar{x} = 2.9$   
 $S_x =$  Blank  
 $n = 1$

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Complete the chart below:

$x$	$P(x)$	$xP(x)$	$x^2P(x)$
1	.2	.2	.2
2	.5	1.0	2.0
3	.3	.9	2.7

1)  $\sum P(x) = 1$

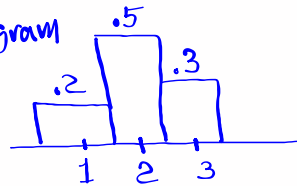
2)  $\sum xP(x) = 2.1$

3)  $\sum x^2P(x) = 4.9$

4) Compute  $\sum x^2P(x) - [\sum xP(x)]^2$   
 $= 4.9 - 2.1^2 = .49$

5)  $\sqrt{\text{Last answer}} = \sqrt{.49} = .7$

6) Draw Prob. dist. histogram  
 $x \rightarrow$  Midpoint  
 $P(x) \rightarrow$  Rel. F.



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Use the chart below for  $x \in P(x)$

$x$	$P(x)$	$xP(x)$	$x^2P(x)$
1	.1	.1	.1
2	.2	.4	.8
3	.3	.9	2.7
4	.4	1.6	6.4

1)  $P(x=2) =$

$1 - [.1 + .3 + .4] =$

$1 - .8 =$   
 $.2$

2)  $\sum xP(x) = 3$

3)  $\sum x^2P(x) = 10$

4) Find  $\sum x^2P(x) - (\sum xP(x))^2$   
 $10 - 3^2 = 1$

5)  $\sqrt{\text{last answer}} = \sqrt{1} = 1$

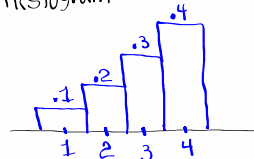
6) Draw Prob. dist. histogram

$x \rightarrow$  L1,  $P(x) \rightarrow$  L2  
 [1-Var Stats] with  
 L1  $\in$  L2 To find

$\bar{x} = 3$

$S_x =$  blank

$n = 1 \leftarrow$  Total Prob.



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For discrete random variable  $x$  with Prob. dist.  $P(x)$ ,

Mean  $\mu$  "mu"  
 Variance  $\sigma^2$  "sigma squared"  
 Standard deviation  $\sigma$  "sigma"

$$\mu = \sum xp(x)$$

$$\sigma^2 = \sum x^2 p(x) - \mu^2$$

$$\sigma = \sqrt{\sigma^2}$$

$x \rightarrow L1$   
 $P(x) \rightarrow L2$   
 Use 1-Var stats  
 with  $L1 \hat{=} L2$

$\mu = \bar{x}$   
 $\sigma = \sigma_x$   
 $\sigma^2 = \sigma_x^2$

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$x$	$P(x)$
2	.1
3	.2
4	.3
5	.2
6	.2

1) verify  $\sum P(x) = 1$   
 $.1 + .2 + .3 + .2 + .2 = 1 \checkmark$

2) Draw Prob. dist. histogram

$x \rightarrow L1, P(x) \rightarrow L2$   
 Use 1-Var stats  
 with  $L1 \hat{=} L2$  to find

Find  $\sigma^2$  in Reduced Fraction

$\mu = \bar{x} = 4.2$   
 $\sigma = \sigma_x = 1.249$   
 $n = 1$

**VARS** **5: Statistics** **4:  $\sigma_x$**   **$x^2$**  **MATH** **1: Frac**

$\sigma^2 = \frac{39}{25}$

**Enter**

Oct 17-7:37 PM

A piggy bank has 3 quarters & 7 Nickels.  
 Take 2 Coins with replacement.

$\left. \begin{matrix} NN \\ NQ \\ QN \\ QQ \end{matrix} \right\}$  Sample Space  
 Complete list of  
 all possible outcomes

$NN \rightarrow 10\phi \quad P(10\phi) = \frac{7}{10} \cdot \frac{7}{10} = .49$   
 $NQ \rightarrow 30\phi \quad P(30\phi) = 2 \cdot \frac{7}{10} \cdot \frac{3}{10} = .42$   
 $QN \rightarrow 30\phi$   
 $QQ \rightarrow 50\phi \quad P(50\phi) = \frac{3}{10} \cdot \frac{3}{10} = .09$

Total	P(Total)
10¢	.49
30¢	.42
50¢	.09

Total  $\rightarrow$  L1      Use 1-Var stats with  
 $P(\text{Total}) \rightarrow$  L2      L1 & L2 to find  
 find  $\sigma^2$  in reduced fraction  $\mu = \bar{x} = 22$   
 $\sigma = \sigma_{\bar{x}} = 12.961$   
 $n = 1$  Total Prob.

VARS 5: Statistics 4:  $\sigma_{\bar{x}}$   $\bar{x}^2$   
 MATH 1: frac Enter  
 $\sigma^2 = 168$

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A piggy bank has 4 dimes & 6 nickels.  
 Take 2 Coins without replacement

$\left. \begin{matrix} NN \\ ND \\ DN \\ DD \end{matrix} \right\}$  Sample Space

$P(NN) = P(10\phi) = \frac{6}{10} \cdot \frac{5}{9} = \frac{1}{3} = \frac{5}{15}$   
 $P(ND \text{ or } DN) = \frac{8}{15}$   
 $P(15\phi) = 2 \cdot \frac{6}{10} \cdot \frac{4}{9} = \frac{8}{15}$   
 $P(DD) = \frac{4}{10} \cdot \frac{3}{9} = \frac{2}{15}$

Total	P(Total)
10¢	$\frac{5}{15}$
15¢	$\frac{8}{15}$
20¢	$\frac{2}{15}$

Total  $\rightarrow$  L1  
 $P(\text{Total}) \rightarrow$  L2

Use 1-Var Stats  
 with L1 & L2 to find  
 find  $\sigma^2$  in reduced fraction.

$\mu = \bar{x} = 14$   
 $\sigma = \sigma_{\bar{x}} = 3.266$   
 $n = 1$   
 $\sigma^2 = \frac{32}{3}$

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68% Range  $\rightarrow \mu \pm \sigma$

95% Range  $\rightarrow \mu \pm 2\sigma$

99.7% Range  $\rightarrow \mu \pm 3\sigma$

Suppose  $\mu = 40$  &  $\sigma = 8$

68% Range  $\Rightarrow \mu \pm \sigma = 40 \pm 8 \Rightarrow$  32 to 48

Usual Range  $\Rightarrow$  95% Range  $\Rightarrow \mu \pm 2\sigma \Rightarrow 40 \pm 2(8)$   
 $\Rightarrow$  24 to 56

$\bar{x}$  Sample Mean

$S$  Sample Standard deviation

$\mu$  Population Mean

$\sigma$  Population Standard deviation

Oct 17-8:21 PM

Pay me \$5, I give you a ticket

Suppose I sell 100 tickets

we draw 1 Ticket, owner gets a Calc.  
worth \$100.

my Net gain | P(my Net gain)

5 - 100	1/100	winning TKT
5 - 0	99/100	losing TKTS

L1	L2
5 - 100	1/100
5 - 0	99/100

Use 1-Var stats with

L1  $\hat{=}$  L2 to find

$\mu = \bar{x} = 4$

Expected Value  
Per Ticket.

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Clarice is going on a trip.

she buys insurance for her luggage for \$100.

Any damages to her luggage, Airline pays her \$1000.

Prob. of damage is  $0.5\% = .005$

Expected Value for airline per policy sold.

Net gain	P(Net gain)	
100 - 1000	.005	damages
100 - 0	.995	No damages

Net gain  $\rightarrow$  L1  $\Rightarrow$  E.V. =  $\mu = \bar{x} = \boxed{\$95}$   
 P(Net gain)  $\rightarrow$  L2

1-Var Stats with L1 & L2

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Pay me \$10, Draw a Card from an ordinary deck of playing cards.

If You draw Ace  $\rightarrow$  I give You \$20

" " = Face  $\rightarrow$  " " = \$10

Any other Card  $\rightarrow$  I give You nothing

Find Expected Value per bet for the house

Net	P(Net)	
\$10 - 20	$\frac{4}{52}$	Ace
\$10 - 10	$\frac{12}{52}$	Face
\$10 - 0	$\frac{36}{52}$	Any other Card

Net  $\rightarrow$  L1  
 P(Net)  $\rightarrow$  L2  
1-Var stats  
 with L1 & L2  
 Find

Find  $\sigma^2$  in Reduced Fraction

$$\sigma^2 = \frac{6600}{169}$$

SG  
 $14 \approx 15$

E.V. =  $\mu = \bar{x} = \boxed{\approx \$6.15}$

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5 Females & 10 Males

Select 3 people.

FFF	} Sample Space	$P(3 \text{ Females}) = \frac{5^C_3 \cdot 10^C_0}{15^C_3} = \frac{2}{91}$
FFM		
FMF		$P(2F \& 1M) = \frac{5^C_2 \cdot 10^C_1}{15^C_3} = \frac{20}{91}$
FMM		
MFF		$P(1F \& 2M) = \frac{5^C_1 \cdot 10^C_2}{15^C_3} = \frac{45}{91}$
MFM		
MMF		$P(3 \text{ Males}) = \frac{5^C_0 \cdot 10^C_3}{15^C_3} = \frac{24}{91}$
MMM		

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$$\begin{aligned}
 P(\underline{\text{at least 1 Female}}) &= 1 - P(\text{None}) \\
 &= 1 - P(\text{All Males}) \\
 &= 1 - \frac{24}{91} = \frac{67}{91}
 \end{aligned}$$

$$\begin{aligned}
 P(\underline{\text{at least 1 Male}}) &= 1 - P(\text{None}) \\
 &= 1 - P(\text{All Females}) \\
 &= 1 - \frac{2}{91} = \frac{89}{91}
 \end{aligned}$$

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# Females	P(# Females)
3	$\frac{2}{91}$
2	$\frac{20}{91}$
1	$\frac{45}{91}$
0	$\frac{24}{91}$

L1

L2

Find  $\sigma^2$  in Reduced Fraction

$$\frac{4}{7}$$

$\mu = 1$   
 $\sigma = .756$   
 $n = 1$

SG  
14 & 15

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